

Chiral forces: reducing cutoff artifacts

Motivation

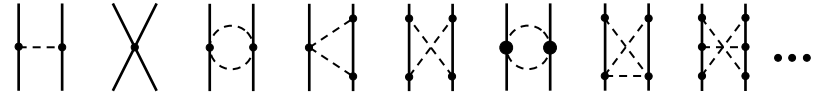
Renormalizable chiral EFT for NN

Local chiral nuclear forces

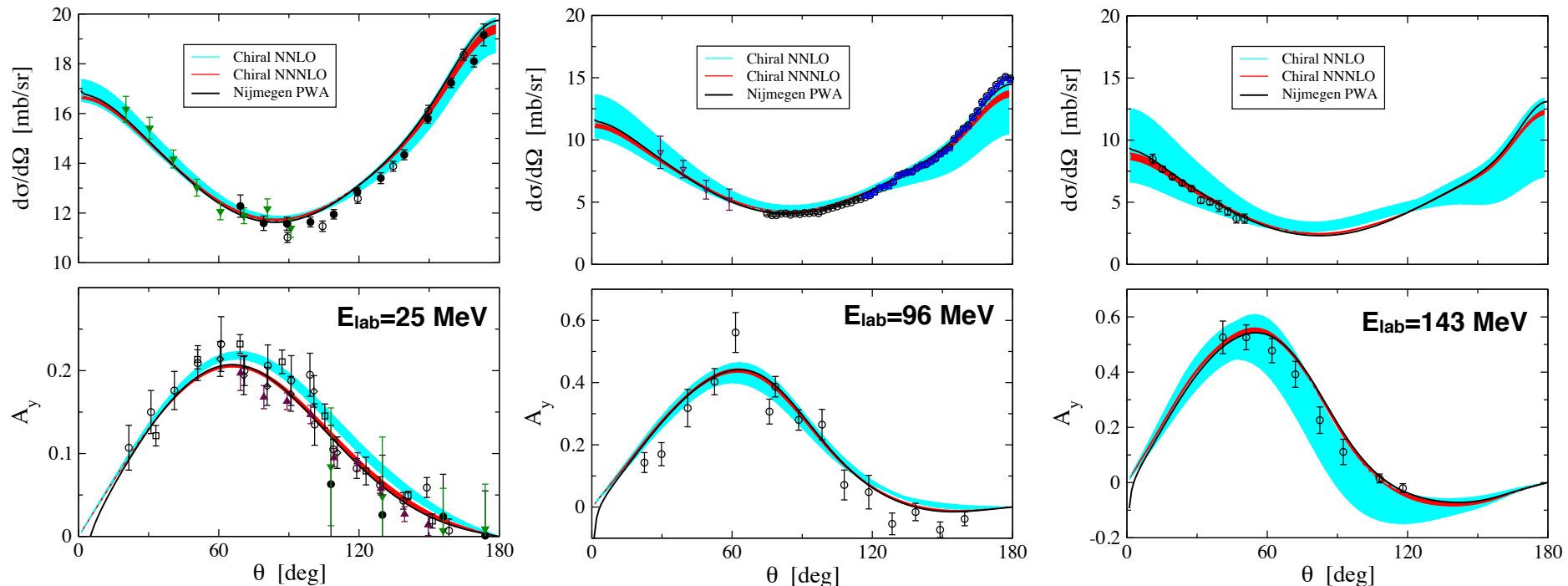
Summary & outlook

Nucleon-nucleon potential at N³LO

- Long-range: parameter-free (all LECs from πN)
- Short-range part: 24 LECs tuned to NN data
- At N³LO, accurate description of NN data up to ~ 200 MeV Entem-Machleidt, EE-Glöckle-Meißner



Neutron-proton diff. cross section & the analyzing power

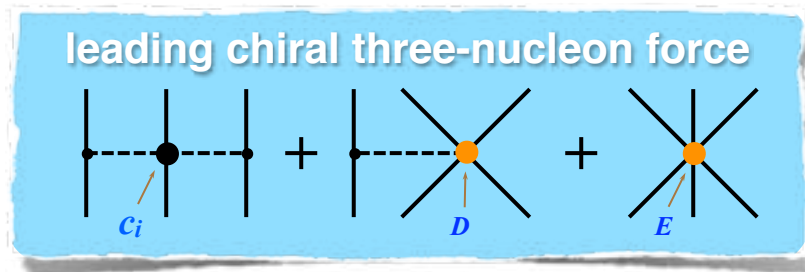


Chiral 3NF & nd elastic scattering

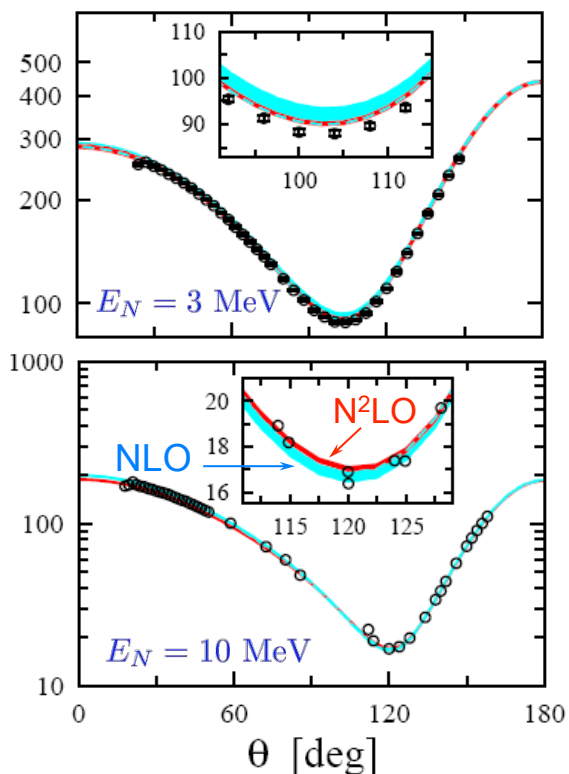
EE, Glöckle, Golak, Kamada, Nogga, Skibinski, Witala

The 3NF starts to contribute at N²LO

The LECs D,E can be fixed e.g. from ³H BE and nd doublet scattering length

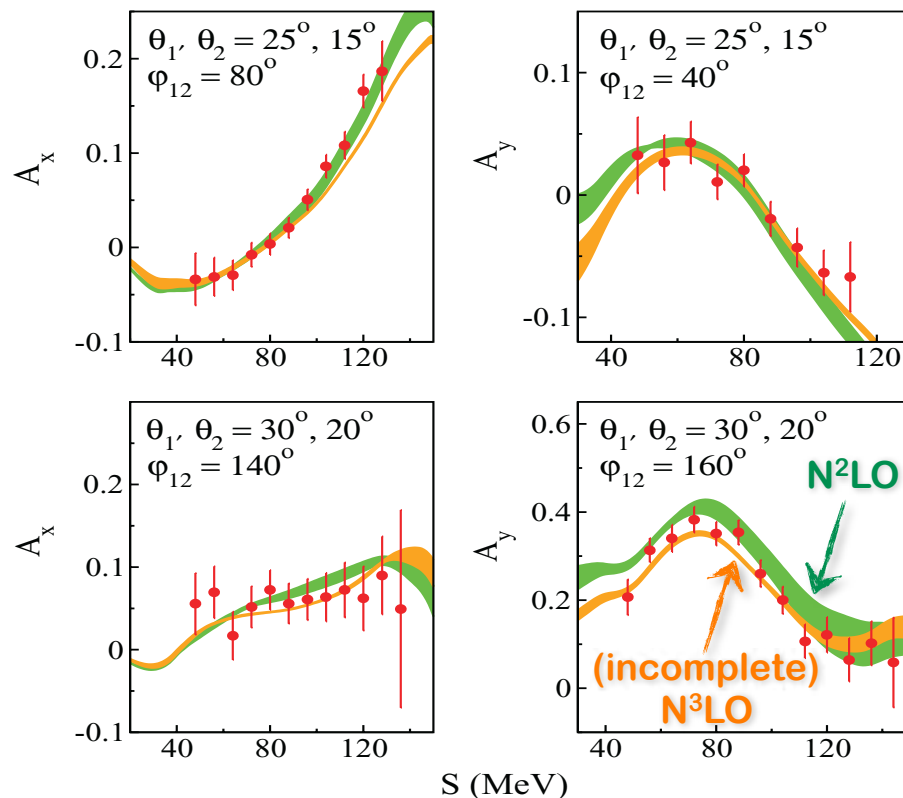


Nd elastic cross sections at low energies



Nd breakup at $E_d=130 \text{ MeV}$

Stephan et al., PRC 82 (2010) 014003



Chiral 3NF & nd elastic scattering

EE, Glöckle, Golak, Kamada, Nogga, Skibinski, Witala

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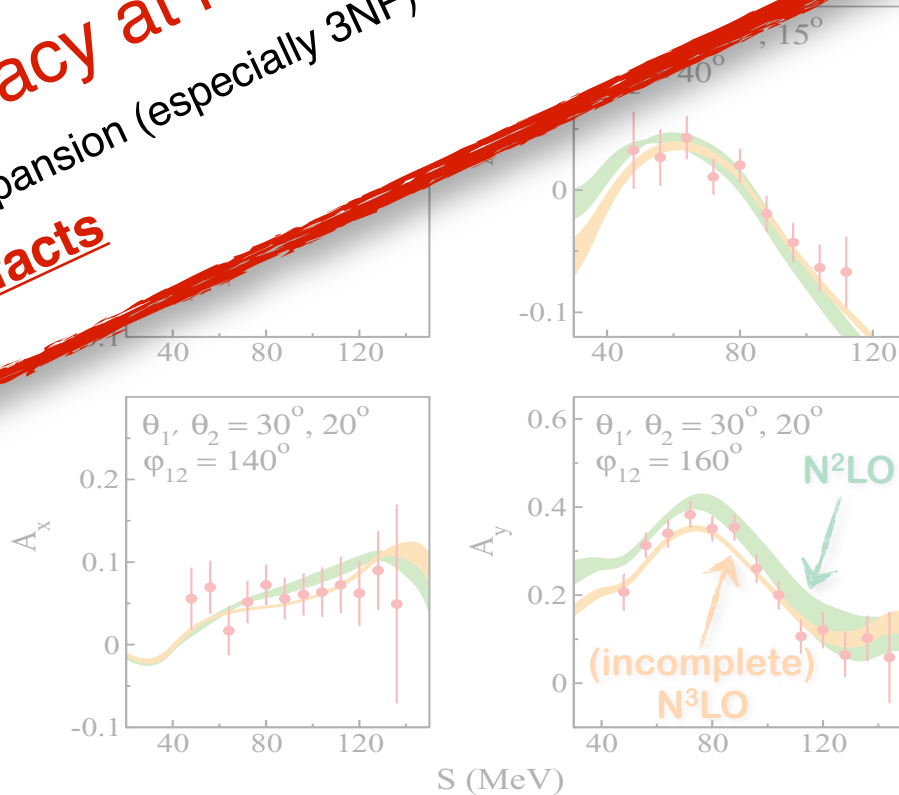
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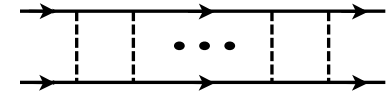
How to increase accuracy at higher energies?
 - go to higher orders in the chiral expansion (especially 3NF)
 - reduce finite-cutoff artefacts



The cutoff issue

Why cutoff?

$$T = \underbrace{V + VG_0T}_{\text{truncated at a given order in the expansion}} = \underbrace{V + VG_0V + VG_0VG_0V + \dots}_{\text{increasingly UV divergent integrals are generated through iterations}}$$



Ideally, would like to calculate the integrals

$$T^{(n)} = V[G_0V]^{n-1} = m^{n-1} \int_0^\Lambda d^3l_1 \dots d^3l_{n-1} \frac{V(\vec{p}', \vec{l}_1) V(\vec{l}_1, \vec{l}_2) \dots V(\vec{l}_{n-1}, \vec{p})}{[p^2 - l_1^2 + i\epsilon] \dots [p^2 - l_{n-1}^2 + i\epsilon]}$$

subtract the UV divergences ($\sim \log \Lambda; \Lambda; \Lambda^2; \dots$) and take the limit $\Lambda \rightarrow \infty$. This is not possible in practice (except for pionless EFT) \longrightarrow let Λ finite and adjust bare C_i to exp data (= implicit renormalization). Λ should be not taken too high [Lepage, EE, Meißner, Gegelia], in practice $\max[\Lambda] \sim 600$ MeV (otherwise spurious BS...)

Price to pay: **finite cutoff artifacts** (i.e. terms $\sim 1/\Lambda; 1/\Lambda^2; 1/\Lambda^3; \dots$), may become an issue at higher energies (e.g. $E_{\text{lab}} \sim 200$ MeV corresponds to $p \sim 310$ MeV/c)

Is it possible to eliminate or at least reduce finite cutoff artifacts?

1st option:

Renormalizable chiral EFT for NN ($\Lambda=\infty$)

Renormalizable chiral EFT for NN scattering

EE, Gegelia PLB 716 (2012) 338

Crucial observation: **non-renormalizability of the LS equation at LO [i.e. $V_{\text{cont}} + V_{\text{OPE}}$] is an artifact of the HB expansion of the propagators**

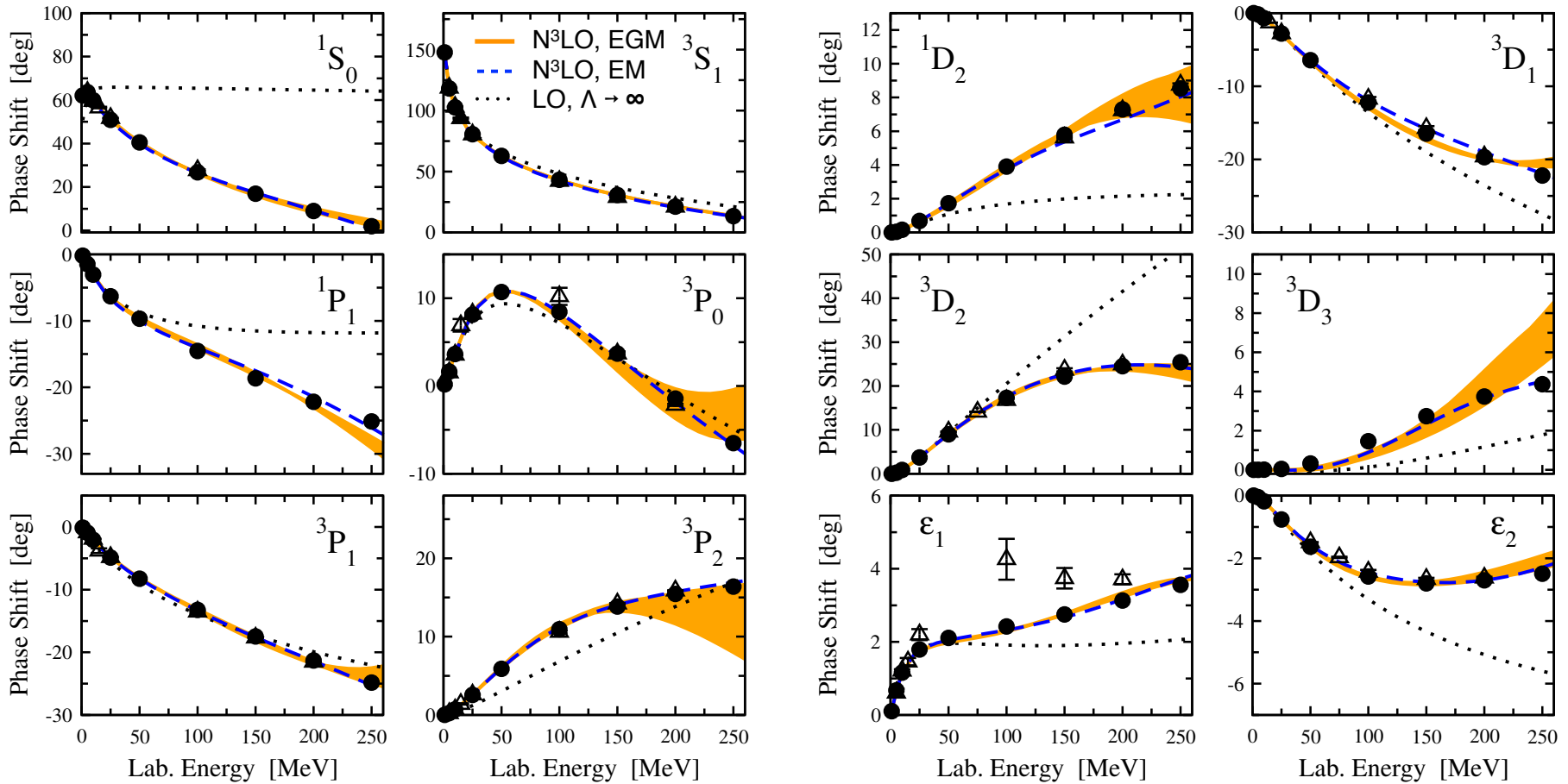
→ do not expand the integrand

→ 3D equations which fulfill relativistic elastic unitarity, e.g.:

$$T(\vec{p}', \vec{p}) = V_{2N}^{(0)}(\vec{p}', \vec{p}) + \frac{m_N^2}{2} \int \frac{d^3k}{(2\pi)^3} \frac{V_{2N}^{(0)}(\vec{p}', \vec{k}) T(\vec{k}, \vec{p})}{(k^2 + m_N^2)(E - \sqrt{k^2 + m_N^2} + i\epsilon)} \quad \text{Kadyshevsky '68}$$

- LO equation is log-divergent (i.e. renormalizable) → can safely take $\Lambda \rightarrow \infty$!
- corrections beyond LO are to be included perturbatively
- power counting is restored by making additional subtractions (EOMS)
- benchmark for perturbative pions: reproduce KSW results EE, Gegelia PLB 716 (12) 338
- parameter-free results for m_q dependence of NN observables at LO EE, Gegelia PoS CD12 (13) 90

Neutron-proton phase shifts



● Higher-order corrections in progress

LETs: perturbative vs non-perturbative pions

Coeff. in the ERE are governed by π 's (LETs): $k \cot \delta = -a^{-1} + \frac{1}{2}rk^2 + v_2k^4 + v_3k^6 + v_4k^8 + \dots$

Predictions for coefficients in the ERE in the 1S_0 channel

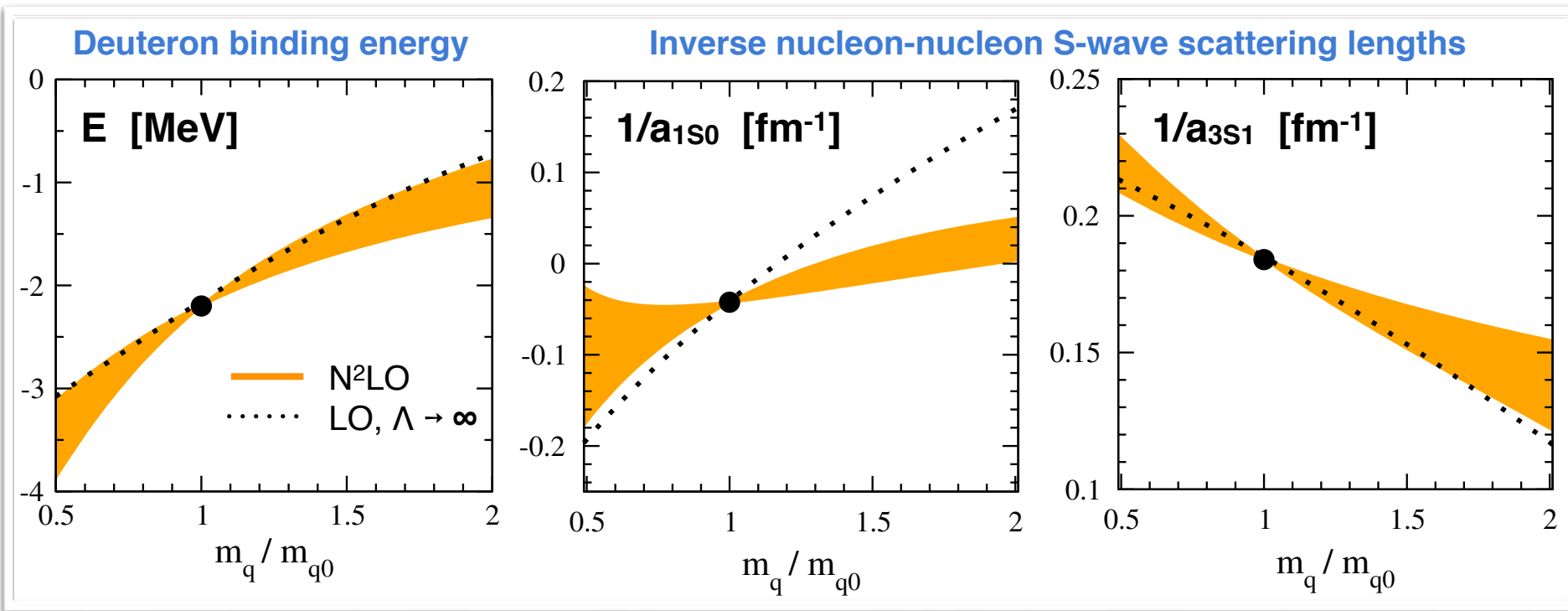
1S_0 partial wave	a [fm]	r [fm]	v_2 [fm ³]	v_3 [fm ⁵]	v_4 [fm ⁷]
NLO KSW from Ref. [23]	fit	fit	-3.3	18	-108
LO Weinberg	fit	1.50	-1.9	8.6(8)	-37(10)
Nijmegen PWA	-23.7	2.67	-0.5	4.0	-20

Predictions for coefficients in the ERE in the 3S_1 channel

3S_1 partial wave	a [fm]	r [fm]	v_2 [fm ³]	v_3 [fm ⁵]	v_4 [fm ⁷]
NLO KSW from Ref. [23]	fit	fit	-0.95	4.6	-25
LO Weinberg	fit	1.60	-0.05	0.8(1)	-4(1)
Nijmegen PWA	5.42	1.75	0.04	0.67	-4.0

Quark mass dependence of the NN force

Berengut, EE, Flambaum, Hanhart, Meißner, Nebreda, Pelaez '13; EE, Gegelia PoS CD12 (13)



In terms of K-factors $K_X^q \equiv \frac{m_q}{X} \frac{\partial X}{\partial m_q} \Big|_{m_q^{\text{phys}}}$

we find:

$$K_{a_s}^q = 2.3_{-1.8}^{+1.9}, \quad K_{a_t}^q = 0.32_{-0.18}^{+0.17}$$

to be compared with earlier calculations: $K_{a_s}^q = 5 \pm 5$, $K_{a_t}^q = 1.1 \pm 0.9$ (W, NLO) EE et al. '03
 $K_{a_s}^q = 2.4 \pm 3.0$, $K_{a_t}^q = 3.0 \pm 3.5$ (KSW, NLO) Beane, Savage '03

Impact on BBN: limits on m_q variation at the time of BBN: $\delta m_q / m_q = 0.02 \pm 0.04$

Deuteron form factors at LO

EE, Gasparyan, Gegelia, Schindler, arXiv:1311.7164 [nucl-th]

Follow the lines of:

Kaplan, Savage, Wise PRC 59 (99) 617

but with nonperturbative pions
and without 1/m-expansion

Interpolating fields for the deuteron:

$$\mathcal{D}_i \equiv N^T P_i N, \quad P_i \equiv \frac{1}{\sqrt{8}} \sigma_2 \sigma_i \tau_2$$

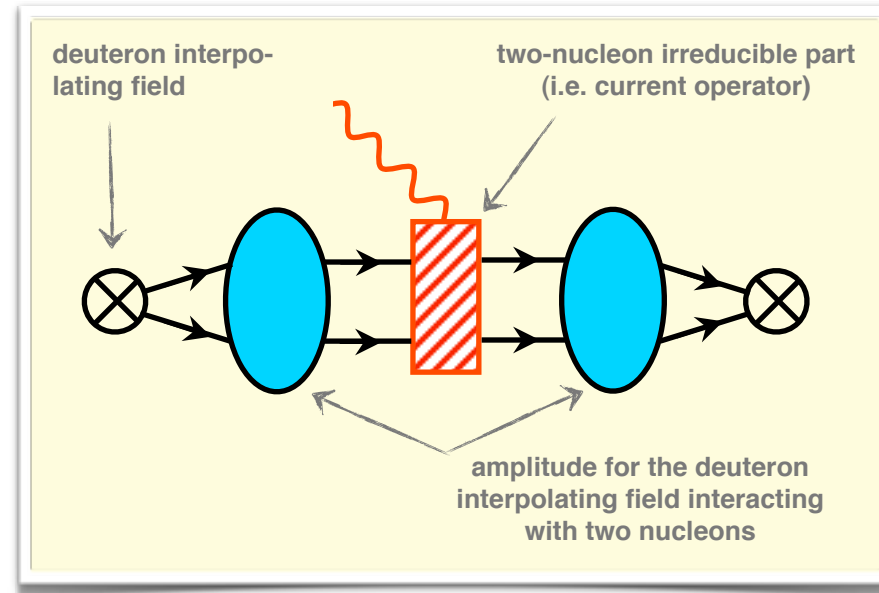
Current MEs in terms of 3-point function (LSZ):

$$\langle \mathbf{P}', j | J_{em}^\mu | \mathbf{P}, i \rangle = -\frac{1}{Z} \left[(P^2 - M_d^2) (P'^2 - M_d^2) G_{ij}^\mu(P, P') \right]_{P^2, P'^2 \rightarrow M_d^2}$$

where $Z = \mathcal{Z}(M_d^2)$ is the residue of the propagator and

$$G_{ij}^\mu(P, P') = \int d^4x d^4y e^{-iP \cdot x} e^{iP' \cdot y} \langle 0 | T \left[\mathcal{D}_i^\dagger(x) J_{em}^\mu(0) \mathcal{D}_j(y) \right] | 0 \rangle$$

← 3-point function

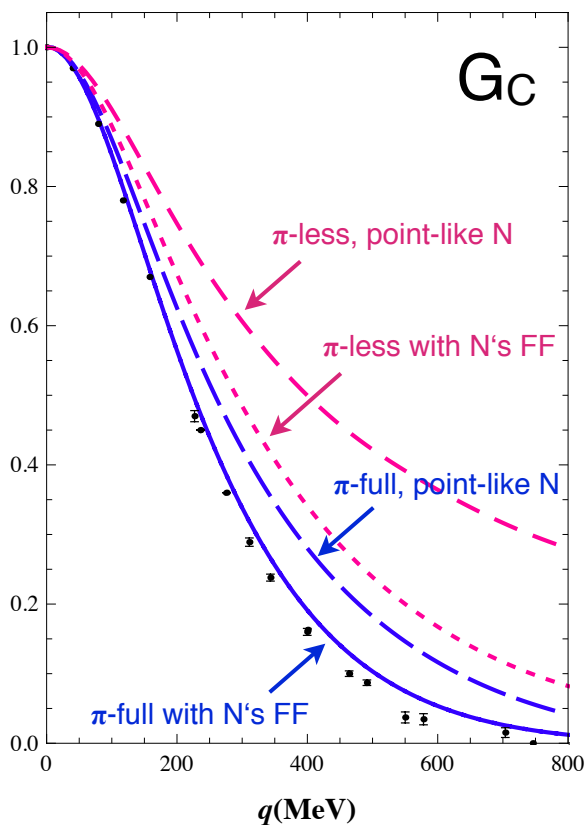


The 3-point function can be expressed in terms of the scattering amplitude obtained by solving the Kadyshevsky equation (solved in 3d without partial wave decomposition)

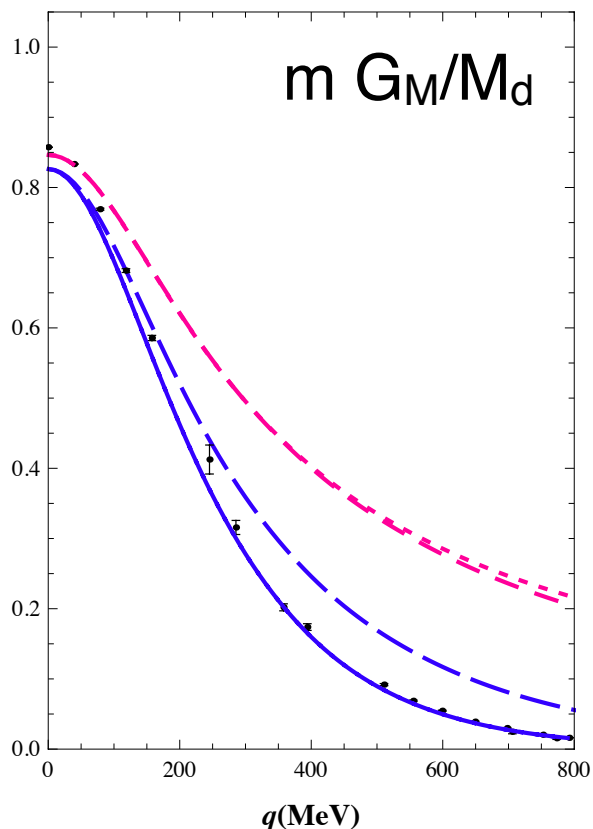
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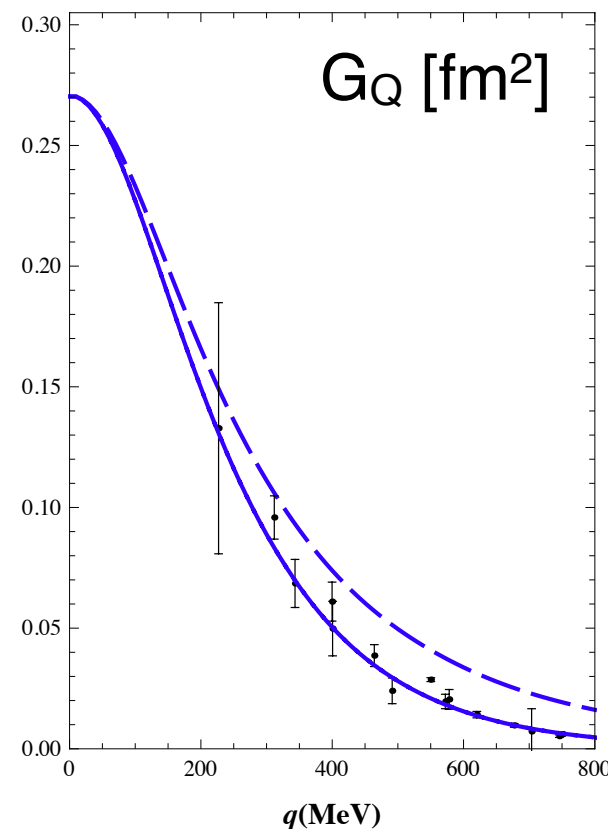
Charge form factor



Magnetic form factor



Quadrupole form factor



Magnetic moment of the deuteron: $\mu^{\text{LO}} = 0.826 (e/(2m))$ to be compared with $\mu^{\text{exp}} = 0.85741 (e/(2m))$

Quadrupole moment of the deuteron: $Q_d^{\text{LO}} = 0.271 \text{ fm}^2$ to be compared with $Q_d^{\text{exp}} = 0.2859 \text{ fm}^2$

2nd option:

Keep Λ finite but reduce Λ -artifacts by a properly chosen regularization

Regularization of the chiral NN potentials

$$\langle \vec{p}' | V^{\text{NNLO}} | \vec{p} \rangle = \left[V_{1\pi}^{(0)} + V_{2\pi}^{(2)} + V_{2\pi}^{(3)} + V_{\text{cont}}^{(0)} + V_{\text{cont}}^{(2)} \right] e^{\frac{-p'^4 - p^4}{\Lambda^4}}$$

order of the chiral expansion

The cutoff Λ should not be chosen too large (spurious bound states, nonlinearities, nonrenormalizable theory) [Lepage'97, EE.](#), [Meißner '06, EE](#), [Gegelia '09](#). On the other hand, smaller values of Λ introduce unnecessary errors.

Typical choice: $\Lambda = 450 \dots 600$ MeV [[N³LO potentials by EGM, EM](#)]

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Claim: while the above nonlocal regulator simplifies the determination of the LECs, it cuts off some model-independent long-range physics one would like to keep and leaves some model-dependent short-range physics one would like to cut off...

Given that $V_{1\pi}^{(0)} + V_{2\pi}^{(2)} + V_{2\pi}^{(3)}$ **is local, local regulator does a better job!**

Reminder:

$$V_{\text{local}}(\vec{p}', \vec{p}) \equiv \langle \vec{p}' | V_{\text{local}} | \vec{p} \rangle = V(\vec{p}' - \vec{p}) \quad \longrightarrow \quad V(\vec{r}', \vec{r}) \equiv \langle \vec{r}' | V | \vec{r} \rangle = \delta^3(\vec{r}' - \vec{r}) V(\vec{r})$$

Regularization of the chiral NN potentials

Peripheral NN scattering as a long-range filter: insensitive to short-range physics and determined by the model-independent long-range interaction ($V_{1\pi}$). Can be computed using Born approximation: $T_{\alpha'\alpha}(p) \equiv \langle p, \alpha' | T | p, \alpha \rangle = \langle p, \alpha' | V_{1\pi} | p, \alpha \rangle$

$$\text{where } V_{1\pi}(\vec{q}) = -\frac{g_A^2}{4F_\pi^2} \frac{(\vec{q} \cdot \vec{\sigma}_1)(\vec{q} \cdot \vec{\sigma}_2)}{\vec{q}^2 + M_\pi^2} \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2$$

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- **Standard, nonlocal regularization** $V_{1\pi}^{\text{reg}}(\vec{q}) = V_{1\pi}(\vec{q}) F\left(\frac{p'}{\Lambda}, \frac{p}{\Lambda}\right)$

Partial-wave decomposition: $\langle p', \alpha' | V_{1\pi}^{\text{reg}} | p, \alpha \rangle = \langle p', \alpha' | V_{1\pi} | p, \alpha \rangle F\left(\frac{p'}{\Lambda}, \frac{p}{\Lambda}\right)$

Regulator affects all partial waves at high momenta independently on α, α'

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- **Local regularization**

$$V_{1\pi}^{\text{reg}}(\vec{q}) = V_{1\pi}(\vec{q}) F\left(\frac{q}{\Lambda}\right) \quad \text{or, alternatively,} \quad V_{1\pi}^{\text{reg}}(\vec{r}) = V_{1\pi}(\vec{r}) F(r/R_0)$$

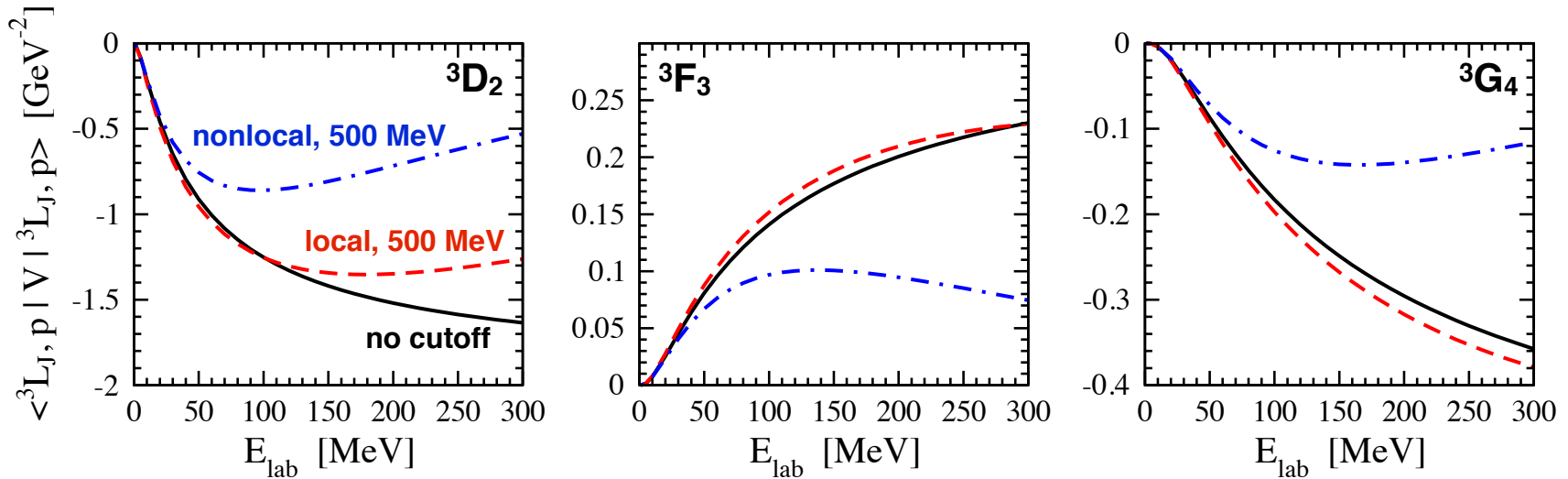
Partial-wave matrix elements in momentum space:

$$\langle p', \alpha' | V_{1\pi}^{\text{reg}} | p, \alpha \rangle \sim \underbrace{\int r^2 dr j_{l'}(p'r) \left[V_{1\pi}^{\alpha'\alpha}(r) F(r/R_0) \right] j_l(pr)}$$

becomes insensitive to F for high l, l'

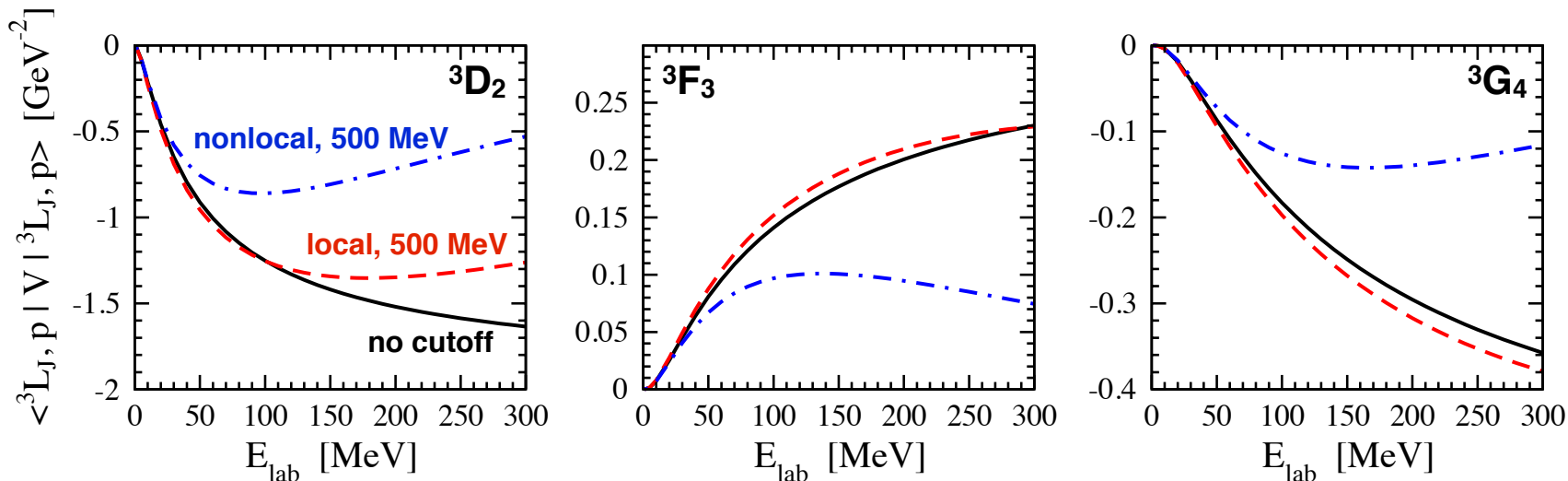
Regularization of the chiral NN potentials

PW projected MEs of the OPEP: $\exp[-(p'^2+p^2)/\Lambda^2]$ versus $\exp[-q^2/\Lambda^2]$ for $\Lambda = 500$ MeV

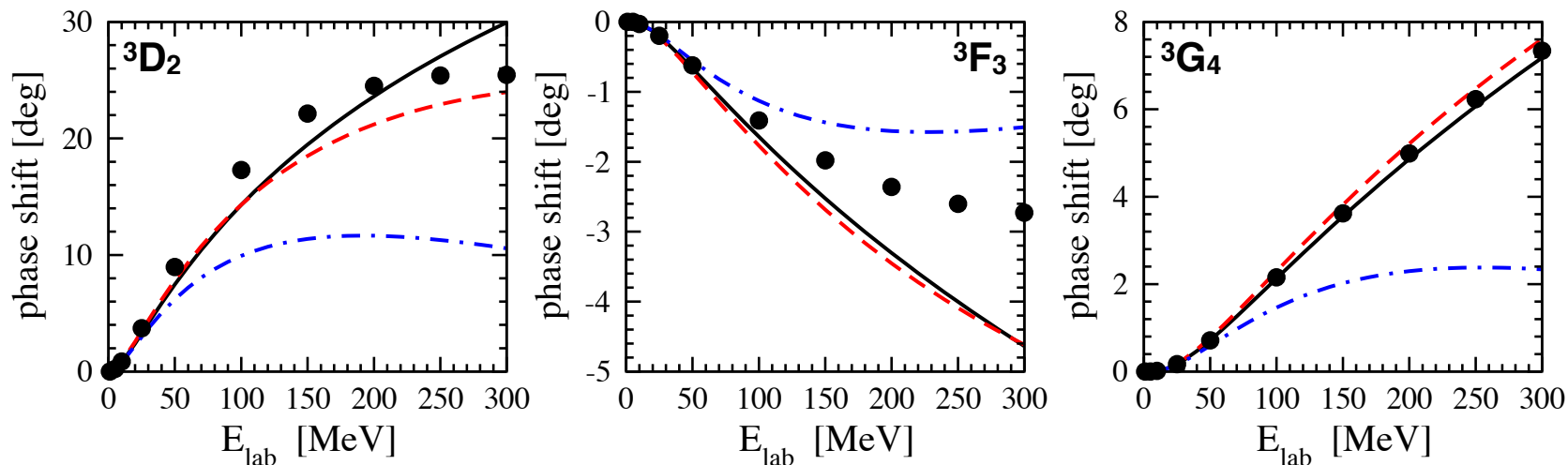


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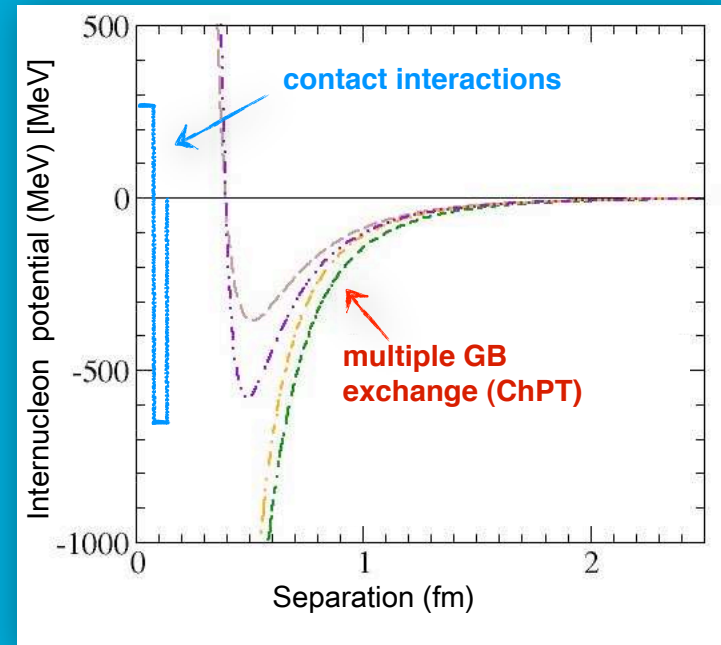


Peripheral partial waves based on the OPE potential (Born approx.)

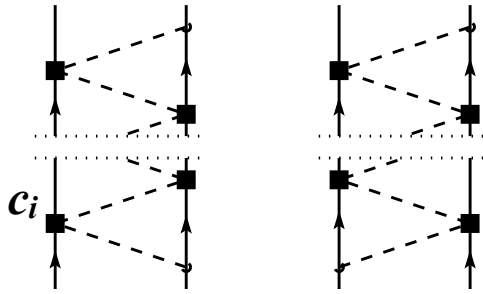


Choice of the cutoff

What is the breakdown distance of the chiral expansion of the multiple-pion exchange ?



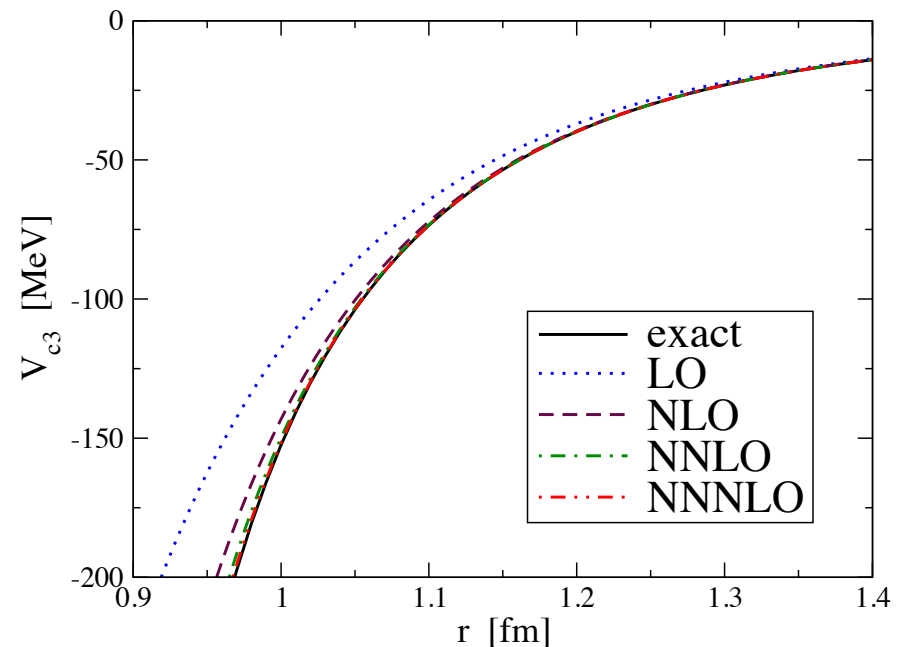
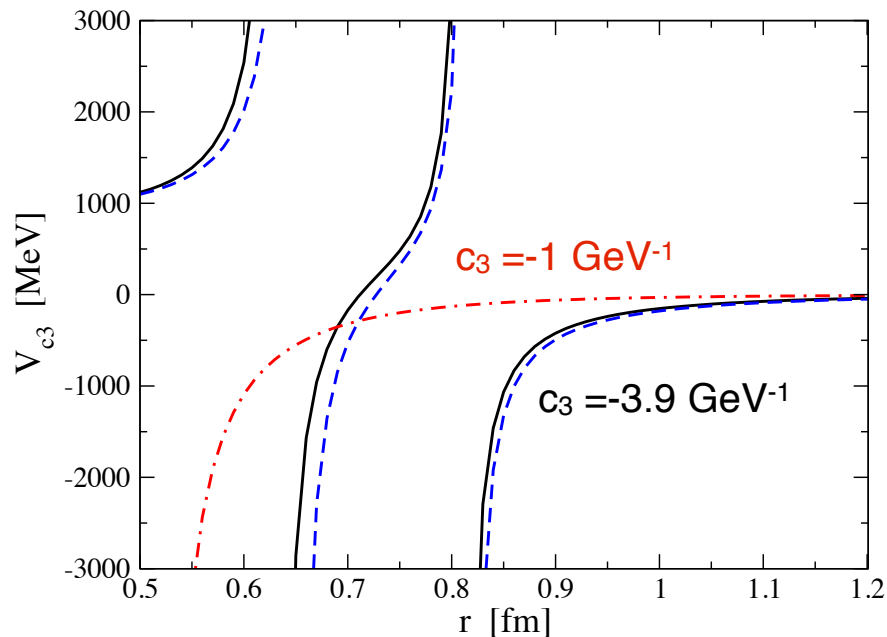
Choice of the cutoff



Certain classes of multiple-pion exchange diagrams (MSS) can be calculated analytically to an infinite order and resummed

Baru, EE, Hanhart, Hoferichter, Kudryavtsev, Phillips, EPJA 48 (12) 69

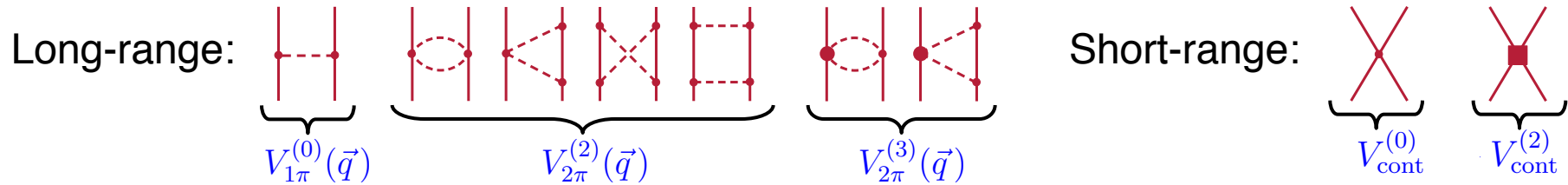
Resummed central potential generated by multi-pion exchange (c_3 -part)



pole(!) at $r \sim 0.81$ fm but good convergence of the chiral expansion for $r > 1$ fm

Construction of the potential

Construction of the potential



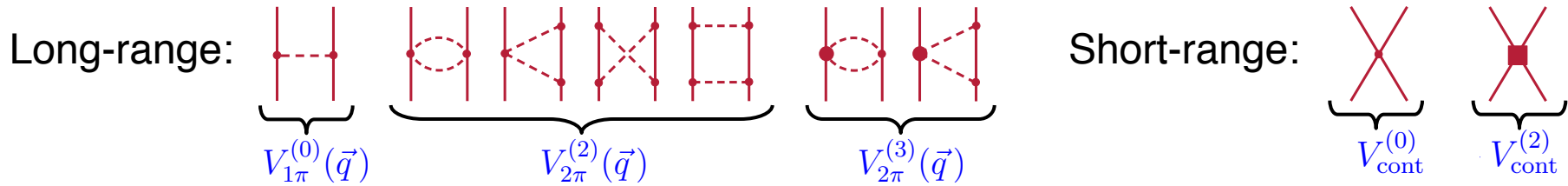
There are 9 isospin-concerning contact terms whose choice is not unique. Standard:

$$V_{\text{cont}}^{(0)} = C_S + C_T(\vec{\sigma}_1 \cdot \vec{\sigma}_2)$$

$$V_{\text{cont}}^{(2)} = C_1 q^2 + C_2 k^2 + C_3 q^2(\vec{\sigma}_1 \cdot \vec{\sigma}_2) + C_4 k^2(\vec{\sigma}_1 \cdot \vec{\sigma}_2) + \frac{iC_5}{2}(\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \vec{q} \times \vec{k} + C_6(\vec{\sigma}_1 \cdot \vec{q})(\vec{\sigma}_2 \cdot \vec{q}) + C_7(\vec{\sigma}_1 \cdot \vec{k})(\vec{\sigma}_2 \cdot \vec{k})$$

$$\text{where } \vec{q} = \vec{p}' - \vec{p}, \quad \vec{k} = (\vec{p} + \vec{p}')/2$$

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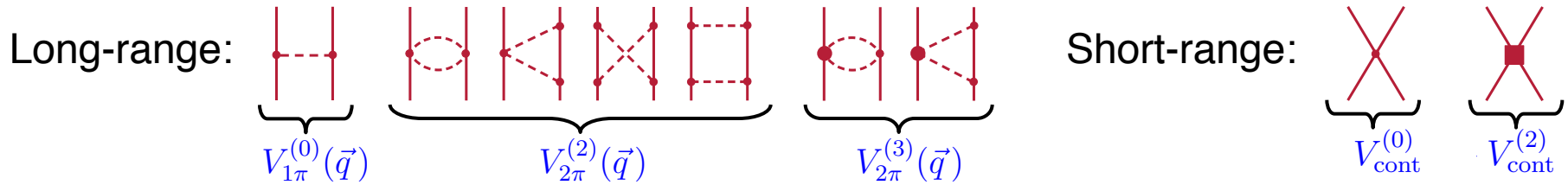
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One can choose instead a **local basis**:

$$V_{\text{cont}}^{(2)} = C_1 q^2 + C_2 q^2(\tau_1 \cdot \tau_2) + C_3 q^2(\vec{\sigma}_1 \cdot \vec{\sigma}_2) + C_4 q^2(\vec{\sigma}_1 \cdot \vec{\sigma}_2)(\tau_1 \cdot \tau_2) + \frac{iC_5}{2}(\vec{\sigma}_1 + \vec{\sigma}_2) \cdot \vec{q} \times \vec{k} \\ + C_6(\vec{\sigma}_1 \cdot \vec{q})(\vec{\sigma}_2 \cdot \vec{q}) + C_7(\vec{\sigma}_1 \cdot \vec{q})(\vec{\sigma}_2 \cdot \vec{q})(\tau_1 \cdot \tau_2)$$

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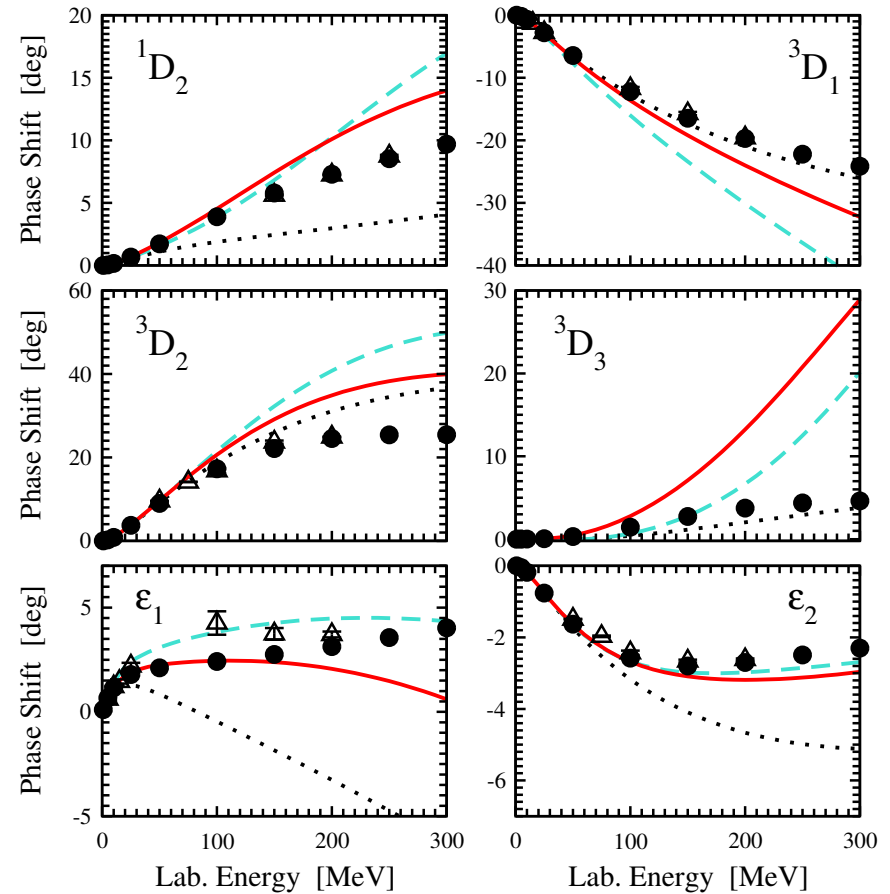
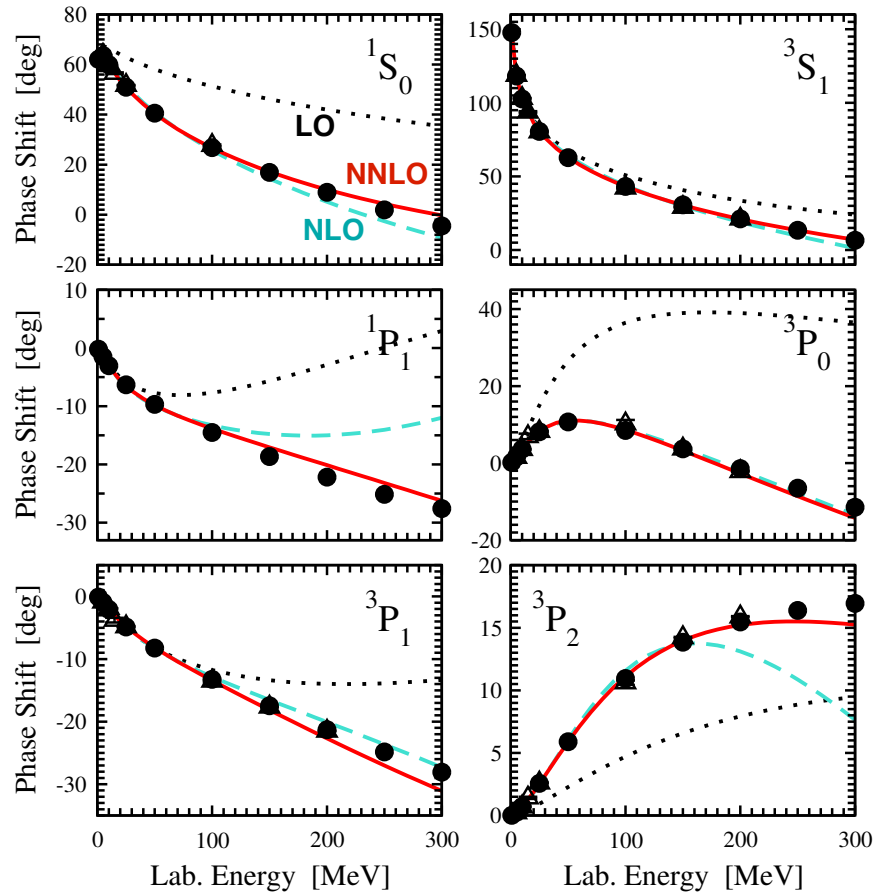
Make Fourier Transform and **regularize in configuration space, e.g.:**

$$V_{\text{long}}(\vec{r}) \rightarrow V_{\text{long}}(\vec{r}) \left[1 - e^{-r^4/R_0^4} \right] \quad \text{and} \quad \delta^3(\vec{r}) \rightarrow \alpha e^{-r^4/R_0^4} \quad \text{where} \quad \alpha = \frac{1}{\pi \Gamma(3/4) R_0^3}$$

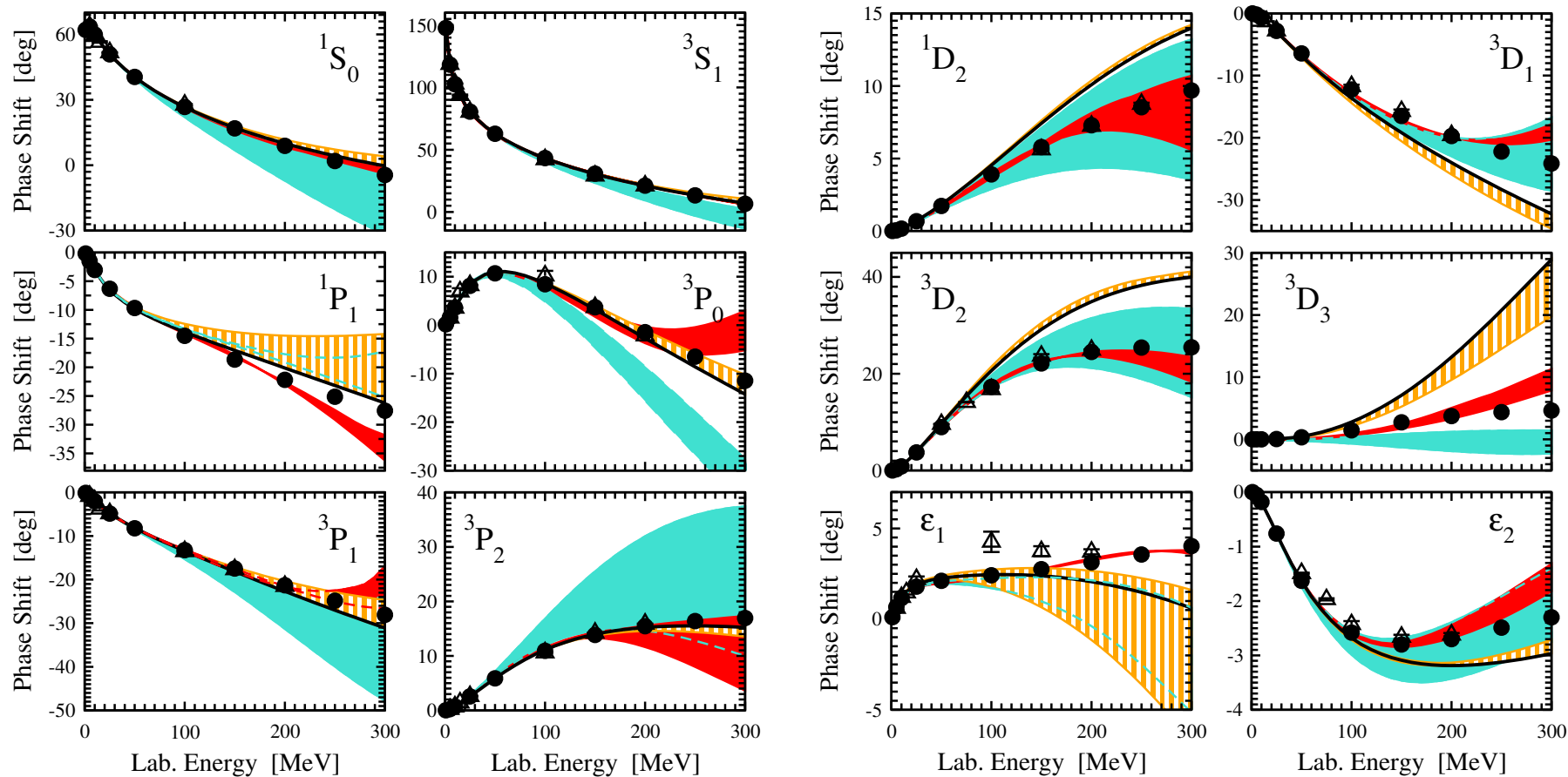
The LECs are determined from NN S-, P-waves and the mixing angle ε_1

Results

np phase shifts: Order-by-order improvement



np phase shifts: Cutoff dependence at NNLO



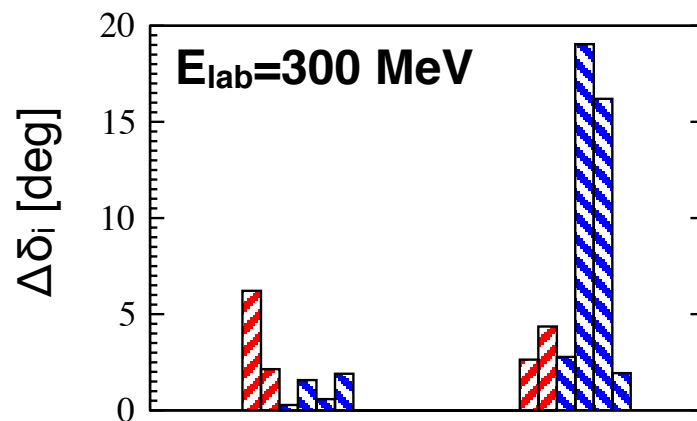
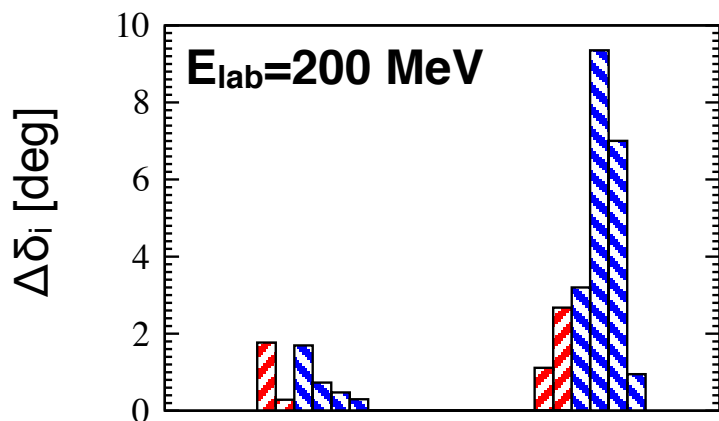
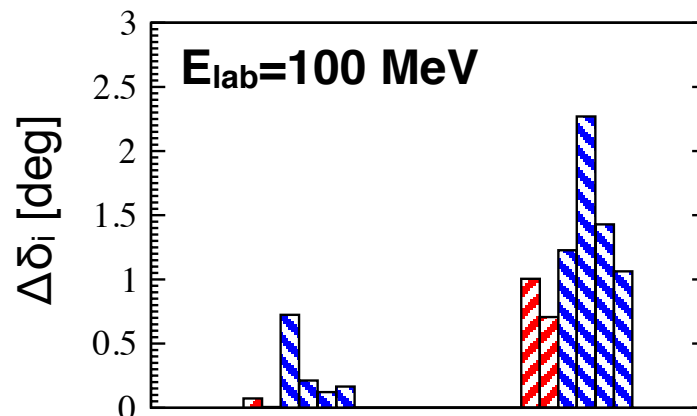
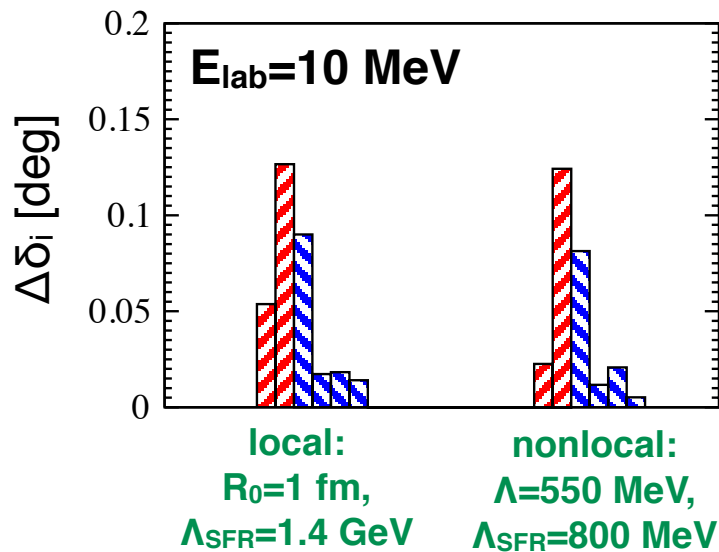
nonlocal N^2LO [EGM]

nonlocal N^3LO [EGM]

local N^2LO , $R_0 = 1...1.2$ fm, $\Lambda_{SFR} = 1...2$ GeV

Error budget: local vs nonlocal regulators

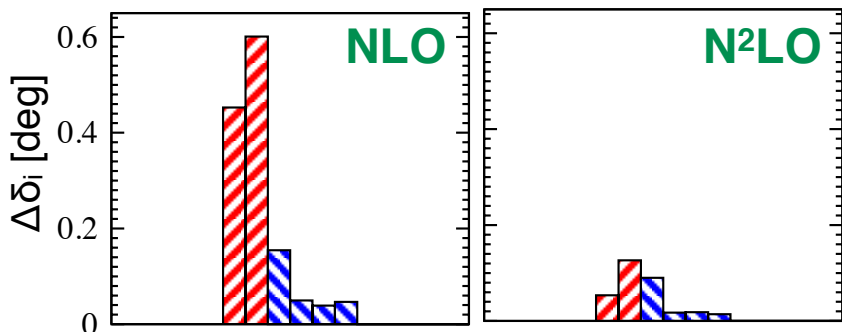
Absolute errors in S- and P-wave phase shifts at N²LO



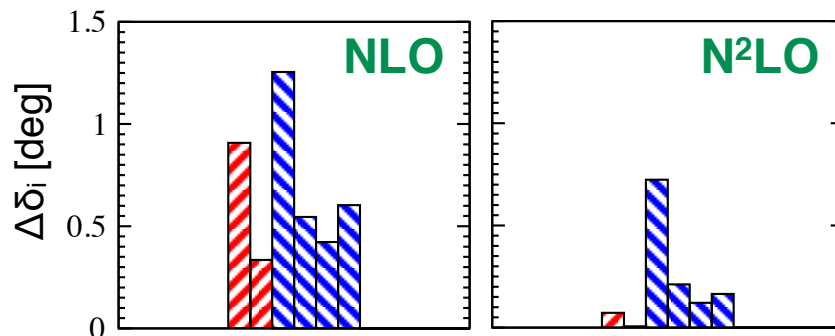
Ordering of partial waves: 1S_0 , 3S_1 , 1P_1 , 3P_0 , 3P_1 , 3P_2

Error budget: NLO vs N²LO (R₀=1 fm, $\Lambda_{\text{SFR}}=1.4$ GeV)

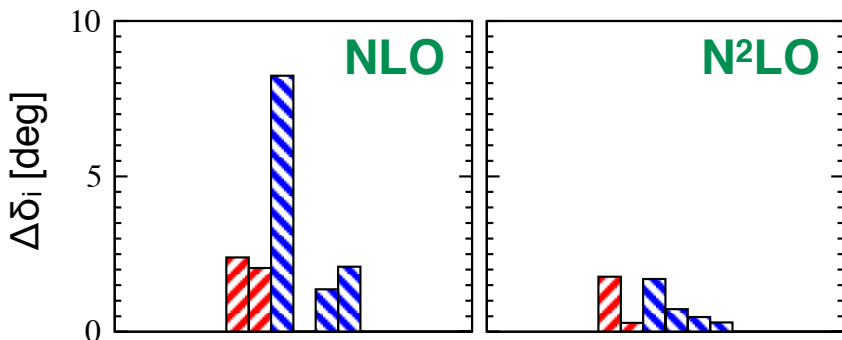
Absolute errors at E_{lab}=10 MeV



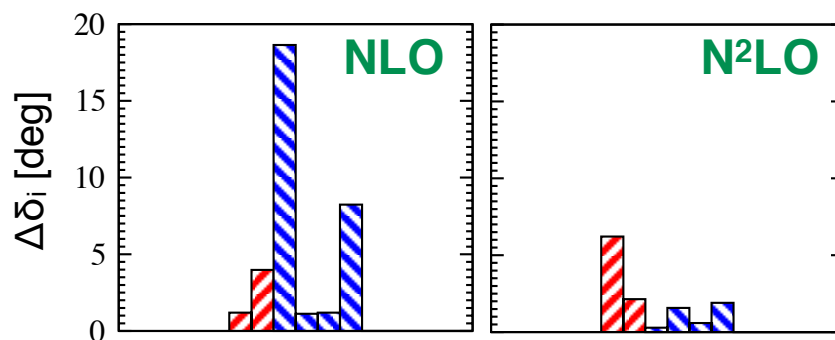
Absolute errors at E_{lab}=100 MeV



Absolute errors at E_{lab}=200 MeV



Absolute errors at E_{lab}=300 MeV

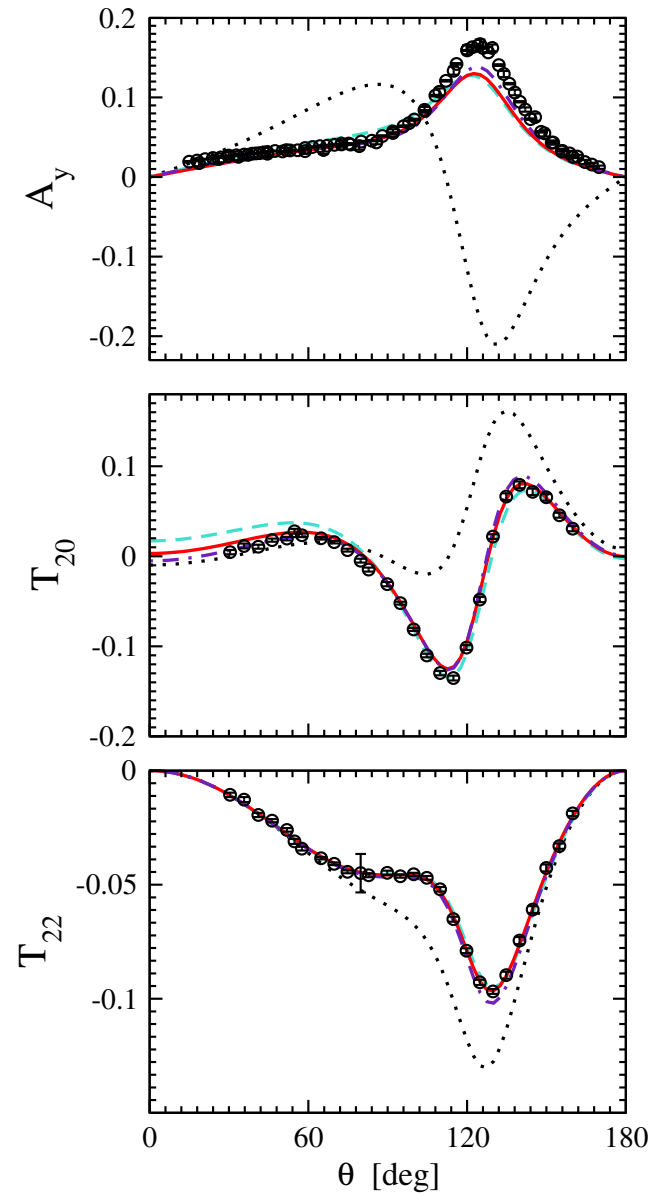
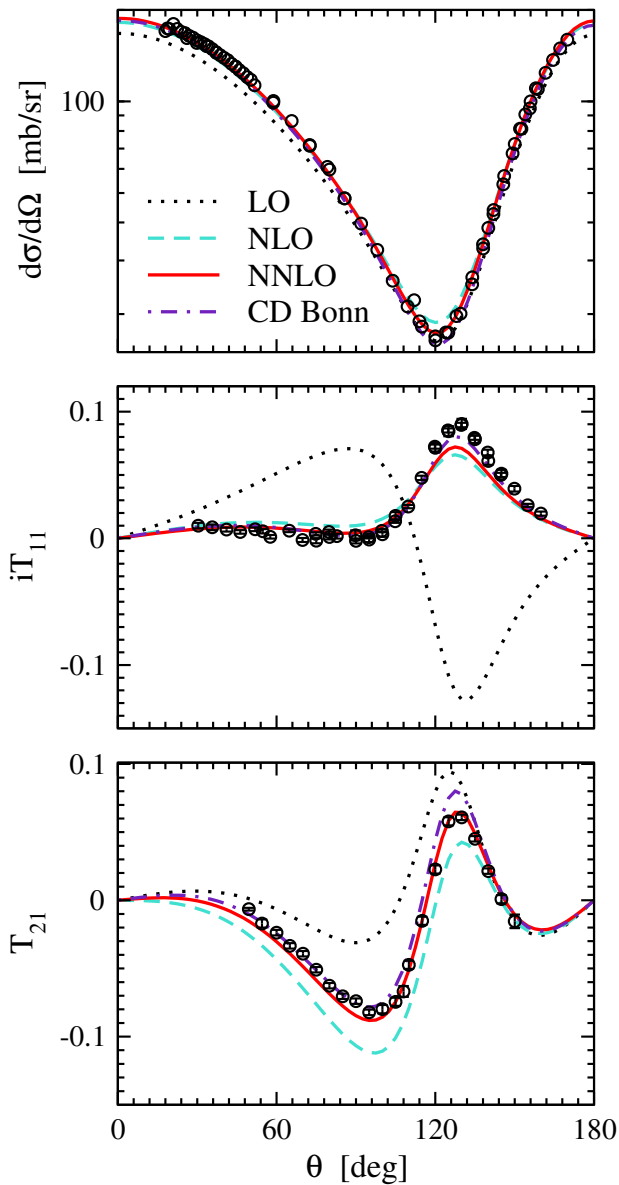


Ordering of partial waves: ¹S₀, ³S₁, ¹P₁, ³P₀, ³P₁, ³P₂

The improvement when going from NLO to N²LO is entirely due to subleading TPEP

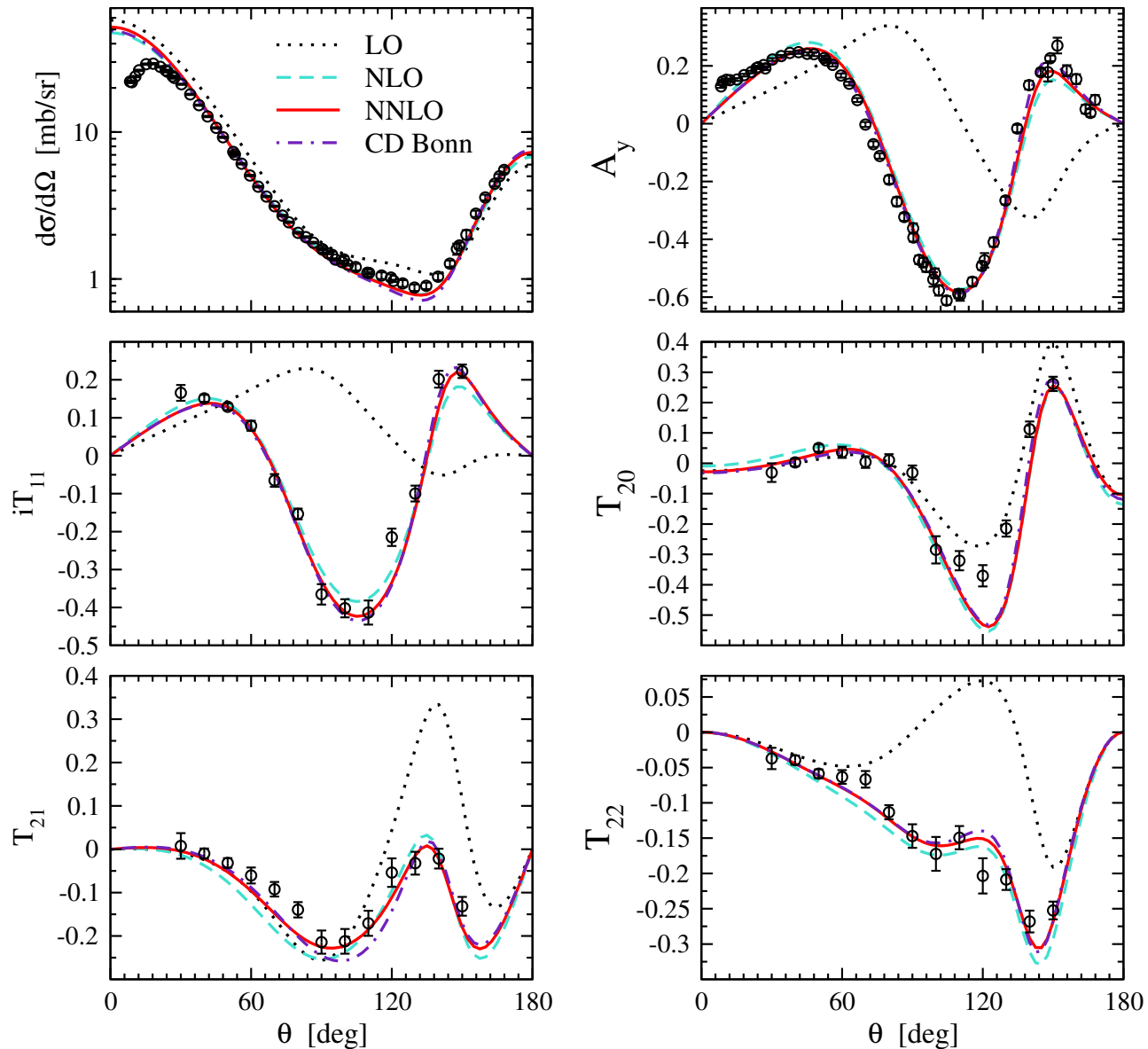
Elastic nd scattering order-by-order

3 MeV:



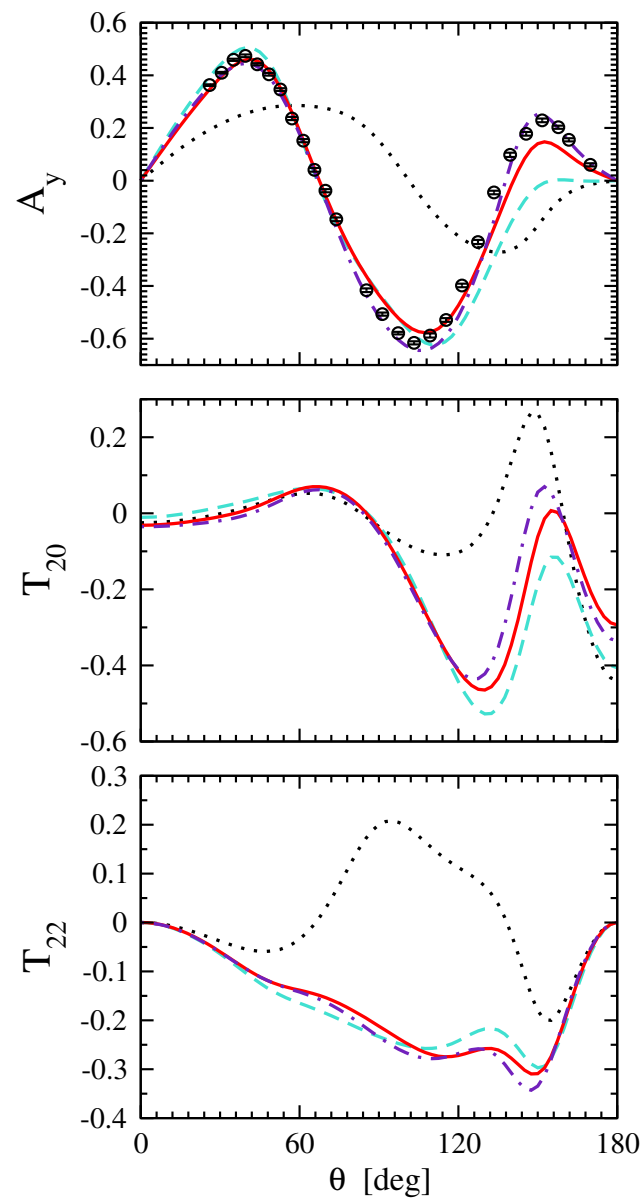
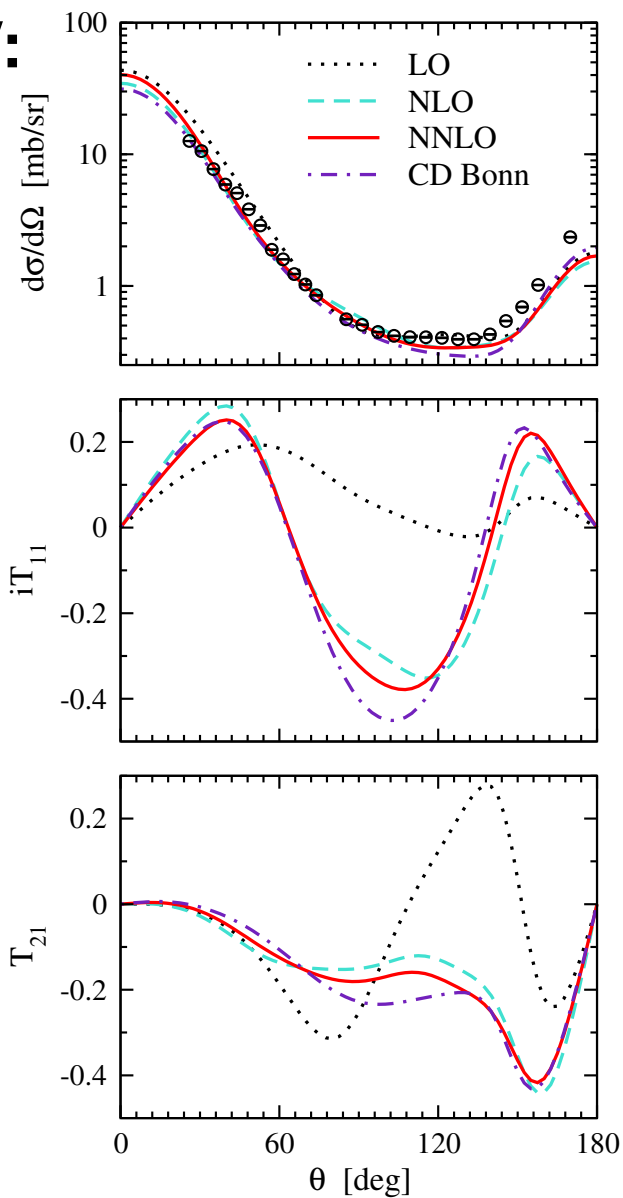
Elastic nd scattering order-by-order

65 MeV:



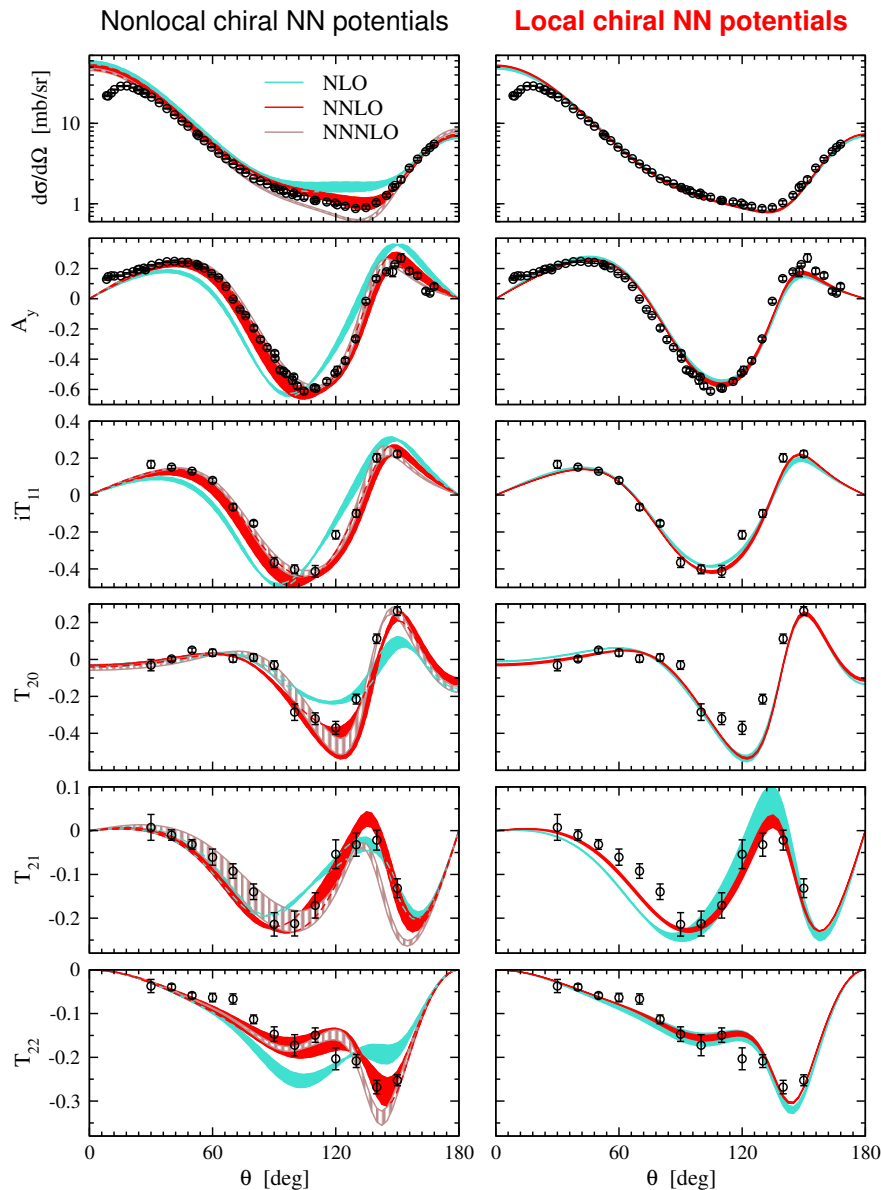
Elastic nd scattering order-by-order

108 MeV:



Elastic nd scattering: Cutoff dependence

65 MeV:



nonlocal NLO/N²LO/N³LO:

$\Lambda = 450 \dots 600$ MeV,

$\Lambda_{\text{SFR}} = 500 \dots 500$ MeV

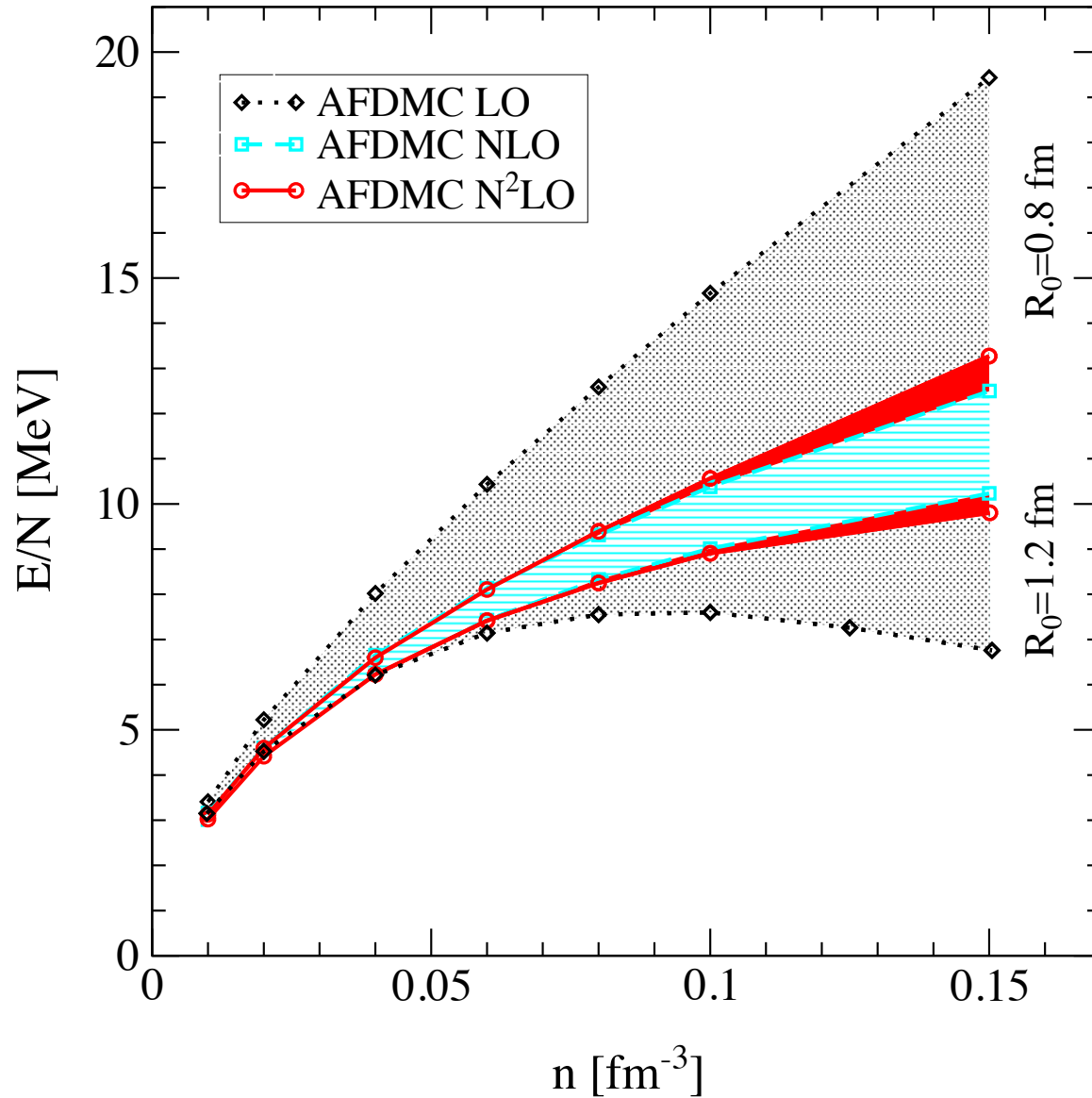
local NLO/N²LO:

$R_0 = 1 \dots 1.2$ fm,

$\Lambda_{\text{SFR}} = 1 \dots 2$ GeV

Neutron matter with local chiral NN forces (QMC)

Gezerlis, Tews, EE, Gandolfi, Hebeler, Nogga, Schwenk, PRL 111 (2013) 032501; in preparation



Summary and outlook

It is possible to eliminate or at least substantially decrease Λ artefacts and thus to considerably increase the applicability range of nuclear chiral EFT!

Renormalizable approach

Summary: Promising results for NN scatt, deut. FF & chiral extrapolations at LO

Pro: Conceptually clean (no cutoff!), well suited for chiral extrapolations

Contra: Derivation of the kernel rather involved (TOPT), cannot directly use in few-/many-body codes (corrections included perturbatively)

To be done: higher orders, strange baryon-baryon systems, 3N,...

Local nuclear forces

Summary: New NN potential at N²LO allows for excellent description of S- and P-waves even at high energies, promising results for 3N scattering

Pro: Transparent physical picture, no need for SFR, can use c_i from π N scattering, can be used in standard codes, accessible for QMC

Contra: Fits require more work, PWD of the 3NF has to be re-done

To be done: Nd with 3NF at N²LO, detailed studies of c_i , explicit Δ , N³LO,...